



Date: 30-10-2018  
Time: 01:00-04:00

Dept. No.

Max. : 100 Marks

**PART A**

Answer ALL questions( 10 ×2 = 20 )

1. Define Total Revenue function.
2. Find the slope of the inclination of the line joining  $(-4,8)$  and  $(8,4)$ .
3. If  $A = \begin{bmatrix} 2 & 5 \\ 1 & 3 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & -1 \\ -3 & 2 \end{bmatrix}$  find  $AB$  and  $BA$ .
4. State Cayley- Hamilton theorem.
5. Define Optimum solution.
6. Explain the Transportation problem.
7. What percent of 4.8 kg is 24 gm.
8. Find the value of  $(45\% \text{ of } 750) - (25\% \text{ of } 480)$ .
9. A person walks 9 hrs at a speed of 3 km per hour and again walks 6 hours at a speed of 4 km per hour. What is the average speed in km per hour.
10. Write the formula for finding the Spearman's rank correlation.

**PART B**

Answer ANY FIVE questions( 5 ×8 = 40 )

11. a) Find the equation of the line whose intercept on the y-axis is 6 and which pass through the point  $(4,-2)$   
b) Find the intercept of the equation  $x + 2y = 3$ . ( 5 + 3 )

12. Prove that 
$$\begin{vmatrix} a+b+2c & a & b \\ c & b+c+2a & b \\ c & a & c+a+2b \end{vmatrix} = 2(a+b+c)^3$$

13. Verify Cayley-Hamilton theorem for the matrix  $A = \begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix}$ .

14. Obtain the initial basic feasible solution by North-West corner rule.

	<b>To</b>				<b>Available</b>
		7	3	2	2
<b>From</b>		2	1	3	3
		3	4	6	5
<b>Demand</b>		4	1	5	10

15. Find the matrix B such that  $A^2 + 3A + B = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$ , where  $A = \begin{bmatrix} 3 & -2 \\ -1 & 4 \end{bmatrix}$ .

16. The average weight of A,B,C is 48 kg. If the average weight of A and B be 40 kg and that of B and C is 43 kg, Find the weight of B.

17. Consider the problem of assigning five jobs to five persons. The assignment costs are given as follows.

		<b>Job</b>				
		<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>
<b>Persons</b>	<b>A</b>	8	4	2	6	1
	<b>B</b>	0	9	5	5	4
	<b>C</b>	3	8	9	2	6
	<b>D</b>	4	3	1	0	3
	<b>E</b>	9	5	8	9	5

18. Find the standard deviation, coefficient of variation and variance.

<b>Age in years</b>	20-30	30-40	40-50	50-60	60-70	70-80	80-90
<b>Number of members</b>	3	61	132	153	140	51	2

**PART C**

Answer ANY TWO questions

( 2×20 = 40 )

19. a) Find the equation of the straight line passing through the points (2, 3) and perpendicular to the line  $x - 2y = 8$ .

b) If  $f(x) = x^2 - 2x + 5$  find  $f(x+2) - f(x+1) + f(x-1)$ .

c) Define equilibrium price, Find the equilibrium price given  $Q_d = \frac{8p}{p-2}$  and  $Q_s = p^2$ .

( 8 + 8 + 4 )

20. a) Find the inverse of the matrix  $A = \begin{bmatrix} 2 & -1 \\ 3 & 2 \end{bmatrix}$ .

b) Solve by using Cramer's rule.

$10x + y + z = 12, \quad 2x + 10y + 3z = 13$  and  $2x + 2y + 10z = 14$ . ( 6+14 )

21. a) Find the solution by Least Cost Method.

		<b>To</b>				<b>Supply</b>
		$D_1$	$D_2$	$D_3$	$D_4$	
<b>From</b>	$S_1$	1	2	1	4	30
	$S_2$	3	3	2	1	50
	$S_3$	4	2	5	9	20
		20	40	30	10	

b) Solve by graphical method

$$\text{Maximize } z = 5x_1 + 4x_2$$

$$1.5x_1 + 2.5x_2 \leq 80$$

$$\text{Subject to } 2x_1 + 1.5x_2 \leq 70 \quad (10 + 10)$$

$$x_1, x_2 \geq 0$$

22. a) Two ladies were asked to rank 7 different types of lipstick. The ranks given by them as follows.

Lipsticks	A	B	C	D	E	F	G
<b>Neela</b>	2	1	4	3	5	7	6
<b>Neena</b>	1	3	2	4	5	6	7

Calculate the Spearman's rank correlation.

b) Ramu was 4 times as old as his son 8 years ago. After 8 years, Ramu will be twice as old as his son. What are their present age.

c) A, B and C started a business by investing Rs1,20,000, Rs 1,35,000 and Rs1,50,000 respectively. Find the share of each, out of an annual profit of Rs56,700.

( 10 + 5 + 5 )

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